

Original Article

# Development of a model selection method based on the reliability of a soft sensor model

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## Abstract

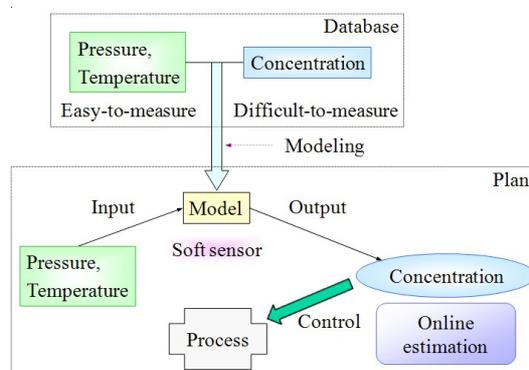
Soft sensors are widely used to realize highly efficient operation in chemical process because every important variable such as product quality is not measured online. By using soft sensors, such a difficult-to-measure variable  $y$  can be estimated by other process variables which are measured online. In order to estimate values of  $y$  without degradation of a soft sensor model, a time difference (TD) model was proposed previously. Though a TD model has high predictive ability, the model does not function well when process conditions have never been observed. To cope with this problem, a soft sensor model can be updated with newest data. But updating a model needs time and effort for plant operators. We therefore developed an online monitoring system to judge whether a TD model can predict values of  $y$  accurately or an updating model should be used for both reducing maintenance cost and improving predictive accuracy of soft sensors. The monitoring system is based on support vector machine or standard deviation of  $y$ -values estimated from various intervals of time difference. We confirmed that the proposed system has functioned successfully through the analysis of real industrial data of a distillation process.

**Keyword:** soft sensor, process control, model selection, time difference, moving window

## 1. Introduction

For realizing highly efficient operations, chemical processes must be controlled by using process variables such as pressure, temperature, concentration, flow, liquid level, and so on. However, every important variable such as product quality is not always measured easily because of technical difficulties, large measurement delays, high investment costs, and others. To estimate the difficult-to-measure variable  $y$ , soft sensors; (Kadlec *et al.*, 2009) are widely used in chemical processes. By using soft sensors,  $y$ -values can be estimated with other process variables  $X$ , which are easily measured online. Figure 1 shows the basic concept of the soft sensors. By using the estimated values, the process can be controlled easily and promptly.

However, soft sensors have some practical difficulties. One of the crucial difficulties is that their predictive accuracy gradually decreases due to changes in the state of chemical plants, catalyzing performance loss, scale deposition, process



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Figure 1. Basic concept of a soft sensor.

drift, and others. In order to reduce the degradation of a soft sensor model, updating models were proposed (Kadlec *et al.*, 2011). These models have high predictive ability because the models are adaptive to new operating conditions. However, the models are optimized for a certain period of operating time, and hence, need to be used carefully. Therefore, operators have to check the model in terms of predictive accuracy of  $y$  for a long period of time and a relationship between  $X$  and  $y$  before practically applied. It takes significant time and efforts because there are many applications of soft sensors.

For solving these problems, Kaneko *et al.* (2011) developed a time difference (TD) model for reducing the efforts of updating models without the degradation of a soft sensor model. Though a TD model has a high predictive ability without updating the model, it does not function well when a process condition has never been observed. In order to cope with both the degradation and efforts for checking the models, we have attempted to develop a model selection method to achieve high predictive ability and reduce the efforts. This method is an online monitoring system to judge whether a TD model can predict values of  $y$  accurately or an updating model should be used for accurate prediction. By using the proposed method, we can reduce maintenance cost, which means time and efforts of detecting and eliminating abnormal data and checking the parameters of the model in model updating, and improve predictive accuracy of soft sensors.

**2. Research Methodology**

In this section, before describing a new model selection method, we briefly explain traditional multivariate statistical process control (MSPC) methods (Kourti, 2005). It is important to find variations in process variables because the prediction accuracy of a TD model is related to process conditions. Then, MSPC methods are applicable to estimate the prediction accuracy of a TD model. Many researchers developed data-based process monitoring methods to detect process variations (Bersimis *et al.*, 2007; Kano *et al.*, 2008). Two types of MSPC methods, the ensemble prediction method (EPM) (Kaneko *et al.*, 2011) and support vector machine (SVM)-based MSPC methods (Kaneko *et al.*, 2009) are used in this paper.

**2.1 EPM**

The EPM handles multiple  $y$ -values predicted by inputting multiple intervals of time difference of  $X$  into a TD model. Figure 2 shows the basic concept of the EPM. To estimate a prediction accuracy of a TD model at time  $k$ , the TD model predicts multiple  $y$ -values from the multiple intervals of time difference of  $X$ ,  $\Delta x(k|k-1)$ ,  $\Delta x(k|k-2)$ , ..., and  $\Delta x(k|k-i)$ . Then,  $\Delta y_{pred}$  values are predicted from each time, and  $y_{pred}$  values are calculated by using  $y(k-1)$ ,  $y(k-2)$ , ..., and  $y(k-i)$  as follows:

$$\begin{aligned}
 y_{pred}(k, k-1) &= \Delta y_{pred}(k, k-1) + y(k-1) \\
 y_{pred}(k, k-2) &= \Delta y_{pred}(k, k-2) + y(k-2) \\
 &\vdots \\
 y_{pred}(k, k-i) &= \Delta y_{pred}(k, k-i) + y(k-i)
 \end{aligned}
 \tag{1}$$

The EPM is calculated by standard deviation of these estimated  $y$ -values. When the EPM values are large, the process is changing and a TD model cannot predict accurately. When the EPM values are small, the process is static state and a TD model can predict accurately. The detail of EPM is written in Kaneko *et al.* (2011).

**2.2 SVM-based MSPC Methods**

Chemical processes are multivariable systems, and hence, it is important to consider a large number of mutually correlated variables. Therefore, MSPC has been developed to monitor such multivariable processes. The basic concept of MSPC is to determine the control limit of process variables, i.e. the normal condition of a process, and to detect data outside the control limit.

SVM is one of the nonlinear classification methods and it can determine the control limit. First, data measured in normal conditions are labeled as 1; data measured in abnormal conditions are labeled as -1; and then, a discriminant model is constructed by using the SVM method with the labeled data. For improving the discriminant ability, principal component analysis (PCA) (Jolliffe, 1986) and independent component analysis (ICA) (Comon, 1994) are combined with the SVM in this study. By using PCA and ICA, we can extract

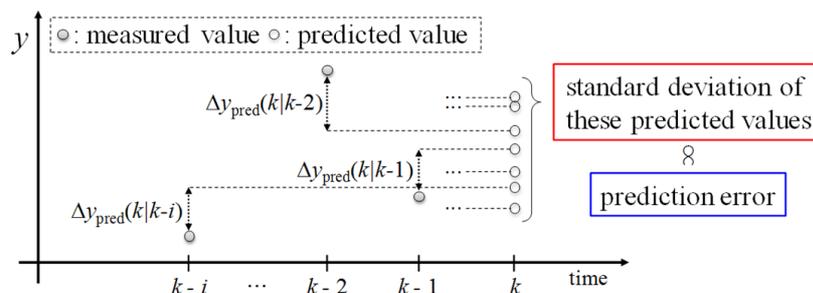


Figure 2. Basic concept of the EPM.

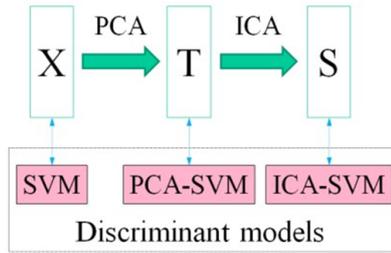


Figure 3. Constructing the discriminant model.

important components from process variables before constructing SVM models. Figure 3 is the image of constructing SVM, PCA-SVM, and ICA-SVM. SVM relates X-variables and the label of data. In PCA-SVM and ICA-SVM, discriminant models are constructed after extracting principal components and independent components from X-variables by using the PCA and ICA methods, respectively.

### 2.3 Proposed method

A TD model is mainly used, but when decreasing the prediction ability of a TD model, a moving window (MW) model (Qin, 1998) is used. A MW model is one of the updating models and used for time series analysis and constructed with the latest data set of X and y. Figure 4 shows the basic concept of the proposed method.

For developing a model discriminating an optimal soft sensor, first, a TD model and a MW model are constructed by training data and prediction error are calculated by using the models. The discriminant model is constructed by using MSPC method between X and the variable that is labeled as 1 when difference of the errors calculated by a TD model and a MW model is higher than a threshold and as -1 when difference of the errors is lower than a threshold. This model discriminates the amount of prediction errors of a TD model. Therefore, this discriminant model judges whether a TD model should be used or not.

In prediction, the discriminant model judges whether a TD model or a MW model should be used for the prediction of new data. When a TD model is selected, the data are predicted by a TD model (not updating). When a MW model is selected, the data are predicted by using a MW model updated by the latest data set. This proposed method will have less frequency of update and high accuracy of prediction.

### 3. Results and Discussion

In this section, SVM, PCA-SVM, ICA-SVM, and the EPM were compared in terms of the detection ratio (DR) and the accuracy ratio (AR) and verified the superiority of the proposed method over traditional soft sensor models with real industrial data. The DR was defined as the ratio of the number of the abnormal data that are detected as abnormal

by a discriminant model and the total number of abnormal data. The AR was defined as the ratio of the number of data that are discriminated correctly and the total number of data.

#### 3.1 Data

The data to estimate performance of soft sensors was obtained from an operation of a distillation column at Mizushima works, Mitsubishi Chemical Corporation. Figure 5 is an image of the distillation column. y-variable was the concentration of the bottom product having a lower boiling point, and X-variables are shown in Table 1. The measurement interval of y was 30 minutes and that of X was 1 minute. The data was collected from monitoring that took place from 2002 to 2006. The training data was measured from January 2002 to December 2003. The test data was measured from January 2004 to December 2006.

#### 3.2 Soft sensor discriminant models

The soft sensor discriminant models were constructed by SVM, PCA-SVM, ICA-SVM, and the EPM. Prediction errors of training data were calculated for the classification. If the absolute difference between prediction error of a TD model and those of a MW model was higher than the threshold 0.3, the data was labeled as -1. If the absolute dif-

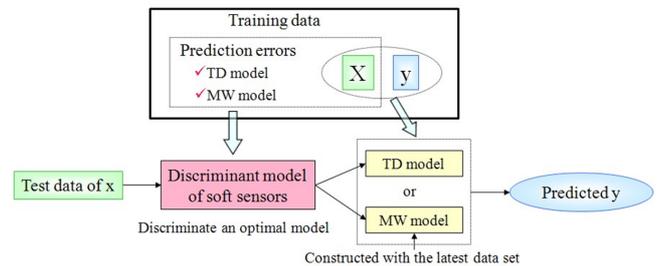


Figure 4. Proposed method.

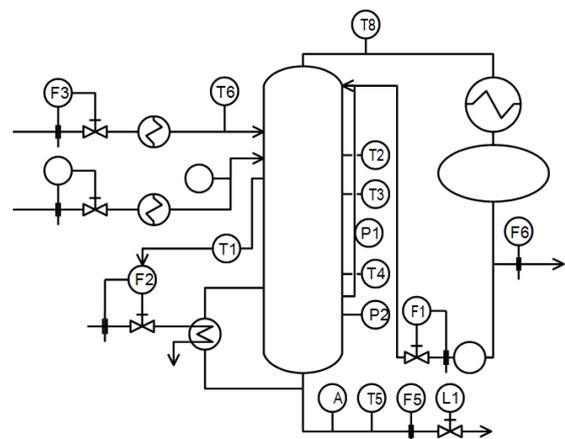


Figure 5. Image of a distillation column.

Table 1. The process variables of distillation column

Symbol		Objective variable
A		Bottom product concentration
No.	Symbol	Explanatory variables
1	F1	Reflux flow
2	F2	Reboiler flow
3	F3	Feed 1 flow
4	F4	Feed 2 flow
5	F5	Bottom flow
6	F6	Top flow
7	L1	Liquid level
8	P1	Pressure 1
9	P2	Pressure 2
10	T1	Temperature 1
11	T2	Temperature 2
12	T3	Temperature 3
13	T4	Temperature 4
14	T5	Bottom temperature
15	T6	Feed 1 temperature
16	T7	Feed 2 temperature
17	T8	Top temperature
18	F4/F3=R	Reflux ratio
19	F1/F6=F	Feed flow ratio

ference was lower than the threshold, the data was labeled as 1. When the threshold is small, the proposed model becomes sensitive to small changes of operation conditions and noise. When the threshold is large, the proposed model can detect only the data that have large prediction errors calculated by the TD model. In this paper, we set the threshold as 0.3, changing the threshold and comparing the prediction errors of test data. The threshold of standard deviation for the EPM was 0.55 decided by the training data. When the standard deviation of a test data exceeds the threshold, a TD model will not predict the data accurately.

Table 2 shows the DR and the AR of test data with the four methods. Though the DR of PCA-SVM and ICA-SVM were improved by using PCA and ICA, there did not seem to be a significant difference of the DR and the AR between SVM, PCA-SVM and ICA-SVM. Meanwhile, the DR and the AR of the EPM were higher than others. Therefore, the EPM was suitable to construct the discriminant model and was used for the following soft sensor analysis.

Table 2. The DR and the AR with the four methods

	SVM	PCA-SVM	ICA-SVM	EPM
DR <sup>a</sup> (%)	47.7	55.9	58.0	77.3
AR <sup>b</sup> (%)	93.5	92.0	90.2	94.2

a : Detection ratio, b : Accuracy ratio.

### 3.3 Soft sensor analysis

Three models were compared as follows; 1. Using only a TD model, 2. Using only a MW model, and 3. Using the proposed method. Figure 6 shows time plots of root mean square error (RMSE). Figure 6(a) was the prediction results of the three methods in the whole time. The horizontal axis was time and the vertical axis was RMSE that was criteria of predictive accuracy of statistical models. The proposed method could reduce the maintenance cost by 8.1% because the MW model was applied to 3,210 data of 39,515 data instead of the TD model. Figure 6(b) and (c) are close-ups of (1) and (2) in Figure 6(a). From Figure 6(b) it can be seen that when RMSE values of the TD model and MW model were almost at same levels, those of the proposed method were close to those of the TD model. This result suggested that the proposed method could keep high predictive ability reducing maintenance cost. Figure 6(c) shows that when RMSE values of the TD model were large, those of the proposal method were close to those of the MW model. This result suggested that the discriminant model detected the time when the state of the plant was different from the past operating conditions under which the TD model was constructed. Then, a MD model was used instead of a TD model for pre-

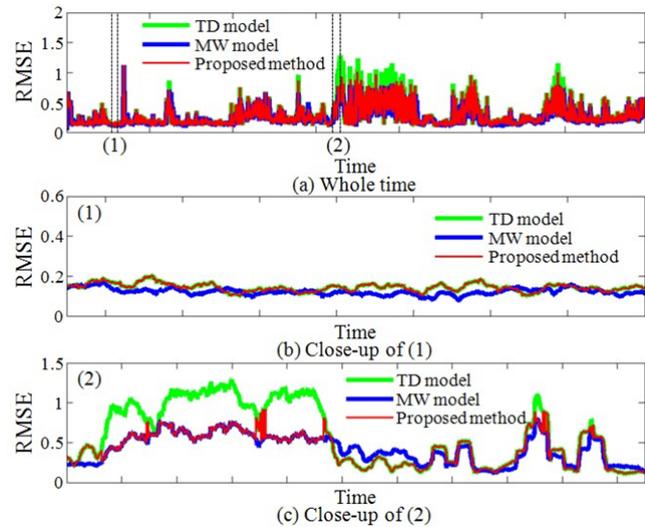


Figure 6. Time plot of RMSE.

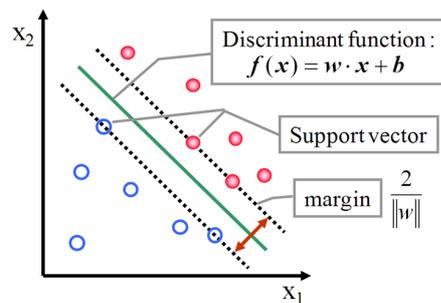


Figure 7. Basic concept of SVM.

dicting the values of  $y$ . When RMSE values of a TD model were small, those of the proposed method were close to those of the TD model. It was conceivable that the MW model was affected by the data where the state of the plant was changing from the process variation to the normal condition.

#### 4. Conclusions

In this work, we developed the discriminant model considering the prediction error of a TD model for high predictive ability and reduction of maintenance cost. The discriminant model judges whether a TD model is reliable in the current operating conditions or not. Through the analysis of the real industrial data, we concluded that the proposed method could reduce maintenance cost and improve predictive accuracy of soft sensors. The proposed system will perform effective operations in chemical plants.

#### Acknowledgements

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#### Appendix A

A support vector machine (SVM) is one of the classification methods used to generate nonlinear classifiers by applying the kernel approach. In a linear SVM, the discriminant function  $f(x)$  is defined as follows:

$$f(x) = Xw + b \quad (\text{A-1})$$

where  $x \in \mathbb{R}^n$  ( $n$  represents the number of variables) denotes a query sample,  $w \in \mathbb{R}^n$ , a weight vector; and  $b$ , a bias. The primal form of the SVM can be expressed as an optimization problem:

Minimize

$$\frac{1}{2} \|w\|^2 + C \sum_i \xi_i \quad (\text{A-2})$$

subject to

$$\begin{aligned} y_i(x_i \cdot w + b) &\geq 1 - \xi_i \\ y_i &\in \{-1, 1\} \end{aligned} \quad (\text{A-3})$$

where  $y_i$  and  $x_i$  represent training data;  $\xi_i$ , slack variables; and  $C$ , the penalizing factor that controls the trade-off between a training error and a margin. By minimizing (A-2), a discriminant model is constructed that shows a good balance between the ability to adapt to the training data and the ability to generalize. In our application, a kernel function is a radial basis function:

$$K(x, x') = \exp\left(-\gamma \|x - x'\|^2\right) \quad (\text{A-4})$$

where  $\gamma$  is a tuning parameter that controls the width of the kernel function. By using (A-4), a nonlinear model can be constructed because the inner product of  $x$  and  $w$  in (A-1) is represented as the kernel function of  $x$ . In this study, we constructed an SVM model that discriminates between target-grade data and off-grade data, and then detected the completion of transition using the discriminant model.